## חATIBIA UПIVERSITY

OF SCIEחCE AחD TECHחOLOGY

Faculty of Health and Applied Sciences
Department of Mathematics and Statistics

| QUALIFICATION: Bachelor of Technology: Accounting and Finance, Advanced Diploma in the <br> Theory of Accounting, Bachelor of Accounting and Diploma in Accounting and Finance |  |
| :--- | :--- |
| QUALIFICATION CODE: 23BACF ;07BACP; <br> O6BDAF; 07ADTA | LEVEL: 5 |
| COURSE: QUANTITATIVE METHODS | COURSE CODE: QTM511S |
| SESSION: July 2019 | PAPER: THEORY |
| DURATION: 3 Hours | MARKS: 100 |


| SUPPLEMENTARY / SECOND OPPORTUNITY EXAMINATION QUESTION PAPER |  |
| :--- | :--- |
| EXAMINER(S) | Mr. A Roux; Ms. S Mwewa; Dr. G Dibaba; Mr. D Ntirampeba |
|  |  |
| MODERATOR: | Mr. J Swartz |


|  | INSTRUCTIONS |
| :--- | :--- |
| 1. Answer ALL the questions. |  |
| 2. Write clearly and neatly. |  |
| 3. | Number the answers clearly. |

PERMISSIBLE MATERIALS

1. Non-Programmable Calculator without the cover

ATTACHMENTS
2. Formula Sheet

THIS QUESTION PAPER CONSISTS OF 4 PAGES INCLUDING THIS FRONT PAGE (Excluding the formula sheet)

## QUESTION 1 [34]

1.1) A company's sales for the years 2001 to 2009 were as follows: ( $x \mathrm{~N} \$ 10000$ )

| Year | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | 2016 | 2017 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sales | 324 | 296 | 310 | 305 | 295 | 347 | 348 | 364 | 370 |

1.1.1) Plot the time series data
1.1.2) Derive, by using the method of least squares, an equation of linear trend for the sales of the company. (Use sequential numbering with $x=1$ in 2009)
1.1.3) Compute trend values for the years 2007 and 2020
1.2) Below are prices of toothpaste, shampoo, cough tablets, and antiperspirant for August 2000 and August 2003. Also included are quantities purchased.

| Item <br> Ingust <br> 2000  August2003  <br>  Price Quantity Price Quantity |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | 2.49 | 6 | 2.69 | 6 |
| Shampoo | 3.29 | 4 | 3.59 | 5 |
| Cough |  |  |  |  |
| tablets | 1.59 | 2 | 1.79 | 3 |
| Antiperspirant | 1.79 | 3 | 2.29 | 4 |

Use 2000 as the base period to compute and interpret the price relatives for 2003 for

### 1.2.1 toothpaste

1.2.2 shampoo
1.2.3 Construct a price index to reflect the overall change in prices of the items purchased for the period 2000-2003. Use the Laspeyres approach. Interpret your price index.
1.2.4) Calculate and interpret the unweighted aggregate price index for 2003 on 2000 as base year.

You win the lottery and get $\$ 100,000$. You decide that you want to invest all of the money in a savings account. However, your bank has two different plans. In 5 years from now, which plan will provide you with more money? Plan 1 The bank gives you a $6 \%$ interest rate and compounds the interest each month. Plan 2 The bank gives you a $6 \%$ interest rate and compounds the interest every 2 months.

## QUESTION 3 [20]

3.1) A sample of 30 delivery times taken by a courier service to deliver parcels from Ongha to Eenhana is shown in the frequency table Below

| Time(minutes) | $5-10$ | $10-15$ | $15-20$ | $20-25$ | $25-30$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 3 | 5 | 9 | 7 | 6 |

Use the data set to calculate and interpret the
3.1.1) Mean
3.1.2) Standard deviation
3.2 During one month, time records show the following results for the number of production workers absent per day :

| 13 | 14 | 9 | 17 | 21 | 10 | 15 | 22 | 19 | 13 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 22 | 13 | 19 | 23 | 17 | 21 | 10 | 9 | 20 | 18 |

For the distribution above, calculate and interpret:
3.2.1) variance
3.2.2) standard deviation
(2)
3.2.3) coefficient of variation

Consider the contingency table below.

|  | Production | Sales | Management | Others | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Undergraduate | 92 | 76 | 24 | 65 | $\mathbf{2 5 7}$ |
| Graduate | 19 | 15 | 62 | 41 | $\mathbf{1 3 7}$ |
| Postgraduate | 15 | 26 | 37 | 28 | $\mathbf{1 0 6}$ |
| Total | $\mathbf{1 2 6}$ | $\mathbf{1 1 7}$ | $\mathbf{1 2 3}$ | $\mathbf{1 3 4}$ | $\mathbf{5 0 0}$ |

If one employee is randomly selected, what is the probability that he or she:
4.1) is either a postgraduate or belongs to sales department?
4.2) is an undergraduate given that he belongs to production department?
4.3) is neither a postgraduate nor belongs to management department?
4.4) does not belong to sales department given that he is not a graduate?

## QUESTION 5 [24]

5.1) Ketu want to be able to withdraw $N \$ 7000$ at the end of five years and withdraw $\mathrm{N} \$ 4000$ at the end of seven years leaving a zero balance in the account after the last withdrawal. If she can earn a simple interest of $6 \%$ p.a. on her balances, how much must she deposit in two years from now to satisfy her withdrawal needs?
5.2) A company considered that a major capital expenditure of $\$ 100,000$ is anticipated in 10 years. What amount does the owner need to deposit annually in the next 10 years in order to accumulate the capital that will be needed to fund such expenditure if the annual interest rate that can be earned is $5 \%$ ?
5.3) An amount was invested on Jan 1, 2015 such that it generated a periodic payment of $\mathrm{N} \$ 2000$ at the end of each month of the calendar year 2015. The annually interest rate on the investment was $13.2 \%$. What was the original investment?
5.4) Solve and graph the following inequality

$$
\begin{equation*}
2(x+5)-60 \leq 5(x-4) \leq 15+2(x+5) \tag{6}
\end{equation*}
$$

# SUMMARY OF FORMULAE QTM511S <br> JUNE/July 2018 EXAM 

Simple Interest:

$$
I=\operatorname{Pr} t
$$

Compound Interest:

$$
A=P(1+i)^{n}
$$

Effective Interest Rate $\quad r_{e f f}=\frac{r}{1-r t}$

Effective Interest Rate

$$
r_{e f f}=\left(1+\frac{r}{m}\right)^{m}-1
$$

Discount

$$
P=A(1-d t) \quad D=A d t
$$

Simple discount Rate $\quad d=\frac{r}{1+r t}$

Nominal Interest Rate

$$
r=m\left[\left(1+r_{e f f}\right)^{\frac{1}{m}}-1\right]
$$

Ordinary Annuity Certain Ordinary Annuity Certain
$S_{n}=R\left[\frac{\left(1+\frac{r}{m}\right)^{n}-1}{\frac{r}{m}}\right]$

$$
A_{n}=R\left[\frac{1-\left(1+\frac{r}{m}\right)^{-n}}{\frac{r}{m}}\right]
$$

Period $t=\frac{\log S-\log P}{m \log \left(1+\frac{r}{m}\right)}$

$$
n=\frac{\log 2}{\log \left(1+\frac{r}{m}\right)}
$$

$$
t=\frac{N-1}{r} \text { for } N \geq 2 n=\frac{\log \left(\frac{i S_{n}}{R}+1\right)}{\log (1+i)} \quad n=-\frac{\log \left(1-\frac{i A_{n}}{R}\right)}{\log (1+i)}
$$

## Measures of Central Tendency



Median

$$
M_{d}=l_{M d}+h\left(\frac{\frac{n}{2}-F}{f}\right)
$$

Mode

$$
M_{0}=l_{M o}+h\left[\frac{f_{1}-f_{o}}{\left(f_{1}-f_{o}\right)+\left(f_{1}-f_{2}\right)}\right],
$$

## Measures of dispersion

Variance $=\frac{\sum f x^{2}-n(\bar{x})^{2}}{n-1}$ or $\quad$ Variance $=\frac{\sum(x-\bar{x})^{2}}{n-1} \quad$ coefficient of variation $=\left(\frac{S}{\bar{x}}\right) \times 100$
Standard deviation $=\sqrt{\text { variance }}$
Quartile

$$
M_{k}=l+\frac{h}{f}\left(\frac{k n}{4}-F\right)
$$

## Index Numbers

Laspeyres price index $=\frac{\sum\left(P_{i} \times Q_{b}\right)}{\sum\left(P_{b} \times Q_{b}\right)} \times 100 \% \quad$ Paasche price index $=\frac{\sum\left(P_{i} \times Q_{i}\right)}{\sum\left(P_{b} \times Q_{i}\right)} \times 100 \%$
Laspeyres quantity index $=\frac{\sum\left(P_{b} \times Q_{i}\right)}{\sum\left(P_{b} \times Q_{b}\right)} \times 100 \% \quad$ Paasche quantity index $=\frac{\sum\left(P_{i} \times Q_{i}\right)}{\sum\left(P_{i} \times Q_{b}\right)} \times 100 \%$

## Time Series

$\hat{y}=a+b x \quad b=\frac{n \sum x y-\sum x \sum y}{n \sum x^{2}-\left(\sum x\right)^{2}} \quad a=\frac{\sum y-b \sum x}{n}$

## Probability

$P(A \cup B)=P(A)+P(B)-P(A \cap B) \quad P(A \cap B)=P(A) P(B)$
$P(B \mid A)=\frac{P(A \cap B)}{P(A)}$

